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PG (CBCS) M.Sc. Semester-IV Examination, 2023 MATHEMATICS PAPER: MTM 403



Full Marks: 50

Time: 2 Hours

 $2 \times 2 = 4$

The figures in the right-hand margin indicate full marks. Candidates are required to give their answers in their own words as far as practicable.

Write the answer for each unit in separate sheet

UNIT: 403.1 MAGNETO HYDRO-DYNAMICS F.M. - 20

1. Answer any TWO from the following questions:

a) Explain the Lorentz Force.

b) What is the current density vector in a medium in motion.

c) Why does MHD wave propagate along longitudinal and transverse directions?

- d) Interpret the pressure term appeared in the equation of conducting laminar viscous flow.
- 2. Answer any **TWO** from the following questions:
 - a) Compare the Maxwell's electromagnetic field equations when the medium is at rest and in motion.
 - b) Write down the equations of motion of a conducting viscous fluid in the presence of a magnetic field.
 - c) State and prove Alfven's theorem.
 - d) Describe the Ferraro's Law of Iso-rotation.
- 3. Answer any **ONE** from the following questions:

 $1 \times 8 = 8$

 $2 \times 4 = 8$

- a) Find the velocity of a viscous conducting liquid between parallel walls in a transverse magnetic field.
- b) "The magnetic body force is a combination of tension and pressure"- Justify it.

[Internal Assessment- 05]

(P.T.O.)

(1)



UNIT: 403.2 STOCHASTIC PROCESS AND REGRESSION F.M. - 20

4. Answer any <u>**TWO**</u> from the following questions:

 $2 \times 2 = 4$

1×8=8

- a) Write the postulates of poisson process.
- b) Write the transition probability matrix for Gambler's ruin problem.
- c) What is Ergodic process?

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- d) Define Markov chain and order of the Markov chain in stochastic process.
- 5. Answer any <u>**TWO**</u> from the following questions: $2 \times 4=8$
 - a) Suppose that the probability of a dry day following a rainy day is $\frac{2}{3}$ and that the probability of a rainy day following a dry day is $\frac{1}{2}$. If May 11 is a dry day then find the probability that May 13 is dry day.
 - b) Suppose a two-state homogeneous Markov chain has the following transition probability matrix:

$$P = \begin{bmatrix} 1 - a & a \\ b & 1 - b \end{bmatrix}, 0 \le a, b \le 1, |1 - a - b| < 1.$$

Prove that (by using Chapman-Kolmogorov equation) the *n*-step transition probability matrix P(n) is given by

$$P(n) = \begin{bmatrix} \frac{b+a(1-a-b)^n}{a+b} & \frac{a-a(1-a-b)^n}{a+b} \\ \frac{b-b(1-a-b)^n}{a+b} & \frac{a+b(1-a-b)^n}{a+b} \end{bmatrix}.$$

c) Derive the equation of the plane of regression containing three variables.

d) When do you say that a state *j* is accessible from a state *i*? When do you say that the two states *i* and *j* communicate?

6. Answer any <u>ONE</u> from the following questions:

a) Prove that
$$r_{1.23...p} = \left(1 - \frac{|R|}{R_{11}}\right)^{1/2}$$
 where the symbols have their usual meanings

b) Describe the pure birth process and deduce the corresponding Yule-Furry process. What will be the probability generating function for this process?

[Internal Assessment- 05]



(2)