PG (CBCS) M.SC. Semester- III Examination, 2023 MATHEMATICS

PAPER: MTM 305 B

(ADVANCED OPTIMIZATION AND OPERATIONS RESEARCH)

Full Marks: 50

Time: 2 Hours

The figures in the right-hand margin indicate full marks.

Candidates are required to give their answers in their own words as far as practicable.

1. Answer any FOUR questions from the following:

 $4 \times 2 = 08$

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- a) Define goal programming problem.
- b) Write the advantages of revised simplex method.
- c) Write the limitations of Fibonacci searching method.
- d) Write the condition when we have to apply dual simplex method to solve an LPP?
- e) State the integer programming problem.
- f) Explain the deletion of an existing variable from the optimal table of an LPP

2. Answer any FOUR questions from the following:

 $4 \times 4 = 16$

- a) Explain the concepts of deviational variables in goal programming problems.
- b) Is it possible to obtain the optimal integer solution of an IPP after neglecting integer restrictions and round-off the optimal solution of the corresponding LPP? Justify.
- c) Write the steps of Davidson-Fletcher-Powell method.
- d) Maximize $f(x) = \begin{cases} 2x/3, & x \le 3 \\ 5-x, & x > 3 \end{cases}$ in the interval [0,4] by Golden Section method using n = 4.
- e) Explain the effect of adding of an existing variable from the optimal result of an LPP.
- f) Explain the concepts of deviational variables in goal programming problems.

3. Answer any TWO questions from the following:

 $2 \times 8 = 16$

a) Solve the following IPP using branch-and-bound method

Maximize
$$z = 2x_1 + 2x_2$$

subject to $5x_1 + 3x_2 \le 8$

$$x_1 + 2x_2 \le 4$$

 $x_1, x_2 \ge 0$ and are integers

b) Minimize
$$f(x) = \begin{cases} 2\sqrt{x}, & x \le 1 \\ 3-x, & x > 1 \end{cases}$$
 in the interval [0,4] by Fibonacci method using $n = 7$.

- c) Write down the procedure of Golden section method.
- d) Derive the conditions of the range of discrete changes of the component of cost vector of the LPP

 $\label{eq:maximize} \begin{array}{c} \text{Maximize Z=CX}\\ \text{subject to AX=b}\\ \text{and X}{\geq}0 \\ \text{such that the optimal solution does not alter.} \end{array}$



[Internal Assessment- 10 Marks]
