

PG CBCS
M.SC.Semester-II Examination, 2021
(MATHEMATICS)
PAPER: MTM-206
(GENERAL TOPOLOGY)

Full Marks: 20**Time: 1 Hour****Answer any TWO questions from the following:****2×10=20**

1. (a) Is the collection $\tau = \{U: X - U \text{ is finite or empty or } U = X\}$ a topology on X ?
 (b) If L is a straight-line in the plane, describe the topology L inherits as a subspace of $\mathbb{R}_1 \times \mathbb{R}$ and as a subspace of $\mathbb{R}_1 \times \mathbb{R}_1$. In each case is it a familiar topology?
 (c) Show that if X is compact Hausdorff under both τ and τ' , then either τ and τ' are equal or they are not comparable. 2+4+4
2. (a) Show that every metric space is normal.
 (b) Show that the product of two regular spaces is regular. 5+5
3. (a) (i) In the finite complement topology on \mathbb{R} , to what point or points does the sequence $x_n = \frac{1}{n}$ converge?
 (ii) Determine the closure of the following subsets of the ordered square:
 $A = \{x \times \frac{1}{2} : 0 < x < 1\}$,
 $B = \{\frac{1}{2} \times y : 0 < y < 1\}$.
 (b) Let A be a subset of a topological space X . Then show that $x \in \bar{A}$ if and only if every open set U containing x intersects A . (3+2)+5
4. (a) If X is a compact space and Y is a Hausdorff space then any bijective continuous function from X into Y is a homeomorphism.
 (b) If $f: X \rightarrow Y$ is a homeomorphism and $p \in X$ then $f: X - \{p\} \rightarrow Y - \{f(p)\}$ is a homeomorphism.
 (c) By using (b) show that $(0,1)$ is not homeomorphic to $(0,1]$. 4+3+3
