

**PG (NEW) CBCS**  
**M.Sc. Semester-IV Examination, 2019**  
**PHYSICS**  
**PAPER: PHS-402**

Full Marks: 40

Time: 2 Hours

**Use Separate Answer Scripts for each unit**

GROUP-A  
 NUCLEAR PHYSICS-II

Marks-20

Answer 1 and any one from 2 and 3

**1. Answer any five questions.**

**5 × 2 = 10**

- a) Explain why  $1f_{7/2}$  level is in between  $1f_{5/2}$  and  $1d_{3/2}$ . Find spin parity of ground state  ${}_{29}\text{Cu}^{63}$ .
- b) "No excited bound state of Deuteron exists" explain.
- c) Using Bartlett or spin exchange force, show that all triplet states are attractive.
- d) Derive the ground state spin and parity of  ${}_{6}\text{C}^{13}$  using shell model.
- e) Show that in n-p scattering, the K.E. of the system in C.M. frame is  $\frac{1}{2}$  of the K.E. of the system in laboratory frame.
- f) Explain: Scattering cross section and reaction cross section.
- g) Estimate the energy released in binary fission of  ${}_{92}\text{U}^{238}$  nucleus.
- h) Write about the tensor force in Deuteron.

**2. Show that the mean logarithmic decrement in energy of neutron due to collision with the nuclei in a medium is given by**

$$E = 1 + \frac{(A-1)^2}{2A} \ln \frac{A-1}{A+1}$$

How many collisions in graphite ( $\text{C}^{12}$ ) are required to reduce the neutron energy from 1 MeV to 1eV?

(Turn over)



(2)

Write about the moderating ratio.

(6+2+2)

3. Derive the ground state wave function of deuteron considering rectangular potential well and hence derive the depth of the potential well.

Estimate the radius of deuteron.

(4+4+2)

## GROUP-B

## QUANTUM FIELD THEORY

Marks-20

Answer 1 and any one from 2 and 3

## 1. Answer any five questions.

5×2=10

- a) Show how the SU(5) grand unified theory accommodates fractional charges of quarks.
- b) If the Dirac field is quantized according to the Bose-Einstein rather than the Fermi-Dirac statistics, what would be the energy of the field?
- c) Find the Euler Lagrange equations for

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{1}{2}m^2 A_\mu A^\mu$$

where

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$$

- d) What is the time ordering? Write down Feynman propagator in terms of time ordering.
- e) Draw the lowest order Feynman diagram of the Compton scattering between an electron and a photon and write the corresponding amplitude from the Feynman rules of graphs.
- f) Define gauge covariant derivative. Why was it introduced?
- g) The Lagrangian density  $\mathcal{L} = (\partial_\mu \phi^\dagger)(\partial_\mu \phi) - m^2 \phi^\dagger \phi$   
where  $\begin{pmatrix} \phi_1 \\ \phi_2 \end{pmatrix}$  is an SU(2) doublet.

(Turn over)



(3)

Show that Lagrangian density has SU(2) symmetry.

h) Find the Noether currents and charges of the Lagrangian density described in (g).

2. The Lagrangian density of a spinless Schrodinger field  $\psi$  is given by

$$\mathcal{L} = i\psi^\dagger \frac{\partial \psi}{\partial t} - \frac{1}{2m} \nabla \psi^\dagger \nabla \psi - V(r)\psi^\dagger \psi$$

i) Find the equation of motion. (2)

ii) Express the free field  $\psi$  and  $\psi^\dagger$  in terms of creation and annihilation operators and find commutation relation between them. (4)

iii) Calculate the Green function

$$G(x_0, \vec{x}, y_0, \vec{y}) = -i \langle 0 | \psi(x_0, \vec{x}) \psi^\dagger(y_0, \vec{y}) | 0 \rangle \theta(x_0 - y_0) \quad (4)$$

3. a) Obtain the expression of the S-matrix operator in the covariant perturbation theory.

State Wick's theorem to write the time-ordered product of a number of fields in terms of the normal ordered products and the vacuum expectation values of time-ordered products. (5)

b) For e. m. field, prove that

$$[A^\mu(t, \vec{x}), A^\nu(t, \vec{y})] = -i g^{\mu\nu} \delta^{(3)}(\vec{x} - \vec{y}) \quad (5)$$

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