

PG (CBCS)
M.Sc. Semester-IV Examination, 2019
PHYSICS
PAPER: PHS-401

Full Marks: 40

Time: 2 Hours

Use Separate Answer Scripts for each unit

GROUP-A

PARTICLE PHYSICS

Marks-20

Answer question number 1 and any one from the rest.

1. Answer any five questions

5×2=10

a) Classify the following reactions:

i) $\pi^0 \rightarrow p + \pi^-$

ii) $K^0 \rightarrow \pi^+ + \pi^-$

b) Explain spontaneous symmetry breaking in particle Physics.

c) What is G-parity? Where is it conserved?

d) $p^+ + \pi^- \rightarrow n^0 + \gamma + Q$

[Mass in MeV: $\pi^-(139)$, $p^+(938)$, $n^0(939)$]

Calculate the energy of the neutron produced.

e) If a Higg's boson of mass m_H moving with a speed $\beta = v/c$ decays into a pair of photons, then find the invariant mass of the photon pair.f) Find the dimension of adjoint representation of $SU(N)$.g) Show that $s+t+u = \sum_i m_i^2$ where the symbols have usual meaning.

h) $P A^0 P^{-1} = \dots$

$P \vec{A}(x) P^{-1} = \dots$

If $\mathcal{L}_{int} = -h\bar{\psi}\gamma_5\psi\phi$, what is the dimension of h ?2. a) Show that $|K_0\rangle$ and $|\bar{K}_0\rangle$ are not eigen states of the operator CP. Construct eigen states of CP operation from linear superposition of $|K_0\rangle$ and $|\bar{K}_0\rangle$. Find the eigen values also. (5)b) Discuss how the intrinsic parity of π^- can be determined from the reaction $\pi^- d \rightarrow n + n$ (5)3. a) Prove that the quark model predicts the following cross-section relation $\sigma(\Sigma^- n) = \sigma(pp) + \sigma(k^- n) - \sigma(\pi^- p)$ (4)b) Using Young Tableaux method for $SU(3)$ group show that

$3 \otimes 3 \otimes 3 = 10 \oplus 8 \oplus \bar{8} \oplus 1$ (4)

c) What is self energy? Explain with Feynman diagram. (2)

(Turn Over)

GROUP-B

STATISTICAL MECHANICS-II

Marks-20

Answer question number 1 and any one from the rest.

1. Answer any five questions

 $5 \times 2 = 10$

- How is the paramagnetism of conduction electrons different from metallic paramagnetism?
- How does Landau level leads to the quantization of energy?
- Consider N independent spin $\frac{1}{2}$ particles in an external magnetic field. Each spin has a magnetic moment μ . What is the magnetisation of the spins as a function of the external magnetic field and temperature?
- The Bose-Einstein condensation temperature for a Rubidium gas (atomic weight 85.47) is $1.7 \times 10^{-23} \text{K}$. Calculate the number density of the condensate ($N_A = 6.023 \times 10^{23}$, $k_B = 1.381 \times 10^{-23} \text{ J/K}$).
- What do you mean by degenerate Fermi gas?
- Explain qualitatively the idea of Yang-Lee singularity for 1D Ising system.
- Using $\ln Z_G = - \sum_r \ln(1 - \eta e^{-\beta \epsilon_r})$, show that the number of particle in the ground state is $N_0 = \frac{\eta}{1-\eta}$, where η is the fugacity.
- Explain why liquid helium does not solidify in normal atmospheric pressure.

- Consider an ideal Fermi gas of N particles in a volume V and in a magnetic field H at temperature $T=0$. The energy of a particle is $\epsilon = \frac{p^2}{2m} \pm \mu_B H$, where μ_B is Bohr magneton. Give an expression for the chemical potential μ_0 in terms of the number of particles N for vanishing magnetic field.

Write down the Fermi momenta of the spins oriented parallel and anti-parallel respectively to the external magnetic field $H \neq 0$, Find the total energy of the spins oriented parallel and anti-parallel to the external magnetic field.

(4+2+2)

- What is De Hass-van Alphen effect? What is the significance of this? (2)

3.

$$H = -J \sum_{i=0}^N \sigma_i \sigma_{i+1} - h \sum_{i=0}^N \sigma_i$$

- Find the partition function in the $N \rightarrow \infty$ limit.

(Turn Over)

(3)

ii) Hence show that the magnetisation of the system is

$$M = N \frac{\sinh \beta h}{\sqrt{\exp(-4\beta h) + \sinh^2(\beta h)}}$$

Also show that this model, in one dimension, does not exhibit any phase transition at finite temperature ($T > 0$). (2+4)

b) Obtain an expression for the mean energy \bar{E} of the Ising model in 2D when the applied field is zero, using the simplest mean field approximation. Hence show that the heat capacity C_h has the behaviour:

$$\begin{aligned} C_h &= 0 \text{ for } T > T_C \\ &= 3Nk/2, \text{ for } T < T_C \end{aligned}$$

Comment on the nature of singularity at T_C . (4)
